

## Hybridizing a fuzzy multi-response Taguchi optimization algorithm with artificial neural networks to solve standard ready-mixed concrete optimization problems

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### Abstract

In this study, a fuzzy multi-response standard ready-mixed concrete (SRMC) optimization problem is addressed. This problem includes two conflicting quality optimization objectives. One of these objectives is to minimize the production cost. The other objective is to assign the optimal parameter set of SRMC's ingredient to each activity. To solve this problem, a hybrid fuzzy multi-response optimization and artificial neural network (ANN) algorithm is developed. The ANN algorithm is integrated into the multi-response SRMC optimization framework to predict and improve the quality of SRMC. The results show that fuzzy multi-response optimization model is more effective than crisp multi-response optimization model according to final production cost. However, the ANN model also gave more accurate results than the fuzzy model considering the regression analysis results.

*Keywords:* Standard ready-mixed concrete; Multi-response optimization; Taguchi method; Fuzzy TOPSIS; Artificial neural networks.

### 1. Introduction

The standard ready-mixed concrete (SRMC) quality is an important issue in the field of material engineering environment [1, 2]. The SRMC industry has been developing rapidly as a result of social, economic and technological developments, especially in roads, bridges, and high rise buildings. SRMC consists of water, cement, crushed special stone, a chemical admixture, and sand which are called aggregates.

SRMC design and optimization are a time consuming and expensive process.

SRMC must conform to some specifications such as strength and durability during its technological life cycle. The characterization of the most appropriate chemical mixture is an important deal to achieve the desired quality for SRMC [3].

The aim of standardization of concrete mixtures is to determine the optimal concrete composition that provides sufficient quality for special applications. Since SRMC's quality to optimize the chemical mixture is closely related with the prediction of each ingredient's optimal levels that increase its strength along with capability in order to decrease production cost consequently the mixture proportion optimization have both technical and financial aspects.

However, such a thorough optimization and production process of each special SRMC is time consuming, instead of this technique; a two-stage methodology may reduce the workload by determining optimal mixture proportion of the SRMC production process. In this paper, a new model is developed to use in the SRMC mixture optimization process. Since the aim of the developed model is an instant optimization of SRMC composition, the scope of the proposed model is limited to the basic quality characteristics of the SRMCs' performance.

For determining the optimal factor levels on concrete quality, experimental design methodologies such as Response Surface Methodology (RSM), Taguchi Methods and factorial design applications are widely used in literature [4-14]. Multi-Attribute Decision Making (MADM) methods are also combined with Taguchi methods where multiple responses are involved [15-18].

The TOPSIS-Taguchi method is quite a useful method compared to the other MADM-based Taguchi methods, such as GRA (Grey Relational Analysis) and VIKOR (Vlse Kriterijumska Optimizacija I Kompromisno Resenje). The advantages of the TOPSIS (Technique for Order Preference by Similarity to an Ideal Solution) method are simplicity and ability to yield an indisputable preference order [19].

Also, Fuzzy MADM methods are suggested for decision-making problems where imprecision and vagueness are involved in past studies. There are various studies that incorporate a fuzzy logic (FL) into MADM models in literature [20-24]. Furthermore, there are some studies which incorporate artificial intelligent (AI) methodologies into MADM based Taguchi models in literature.

Over the last decades, different AI applications based on FL or Artificial Neural Network (ANN) has become popular and has been used by many researchers for a variety of engineering applications [25]. For example, Tong and Su [24] optimized the multi response problem in the Taguchi method by Fuzzy TOPSIS (FTOPSIS). Lan [26] applied a fuzzy Taguchi deduction optimization on multi-attribute CNC turning.

Sivapirakasam et al. [27] developed a combination of Taguchi and FTOPSIS methods to solve multi-response parameter optimization problems in green manufacturing. Also, ANN's applied to many civil engineering applications such as drying shrinkage [28], ready mixed concrete delivery [29], slump model [30], concrete durability [31], mechanical behavior of concrete at high temperatures [32-34], workability of concrete with metakaolin and fly ash [35, 36], and the long term effect of fly ash and silica fume on compressive strength [37], predicting comprehensive strength and slump for high strength concrete (HSC) [38], drying shrinkage of concrete [39], estimation of compressive strength of self-compacting concrete [40].

This paper argues a new model to predict the optimal mixture dosages of SRMC. The main contribution of this article is to demonstrate the application of hybrid FTOPSIS-Taguchi-ANN model to predict optimal mixture dosage of a SRMC. In the developed model, FTOPSIS based Taguchi is firstly used to identify the optimal mixture dosages of SRMC. Once needed experimental values, according to Taguchi's appropriate orthogonal array, are entered by the user in the FTOPSIS-Taguchi module, the optimal set of mixture dosage levels are determined by this module. However experimental values such as factor levels and test results can be simultaneously transferred to ANN module for the prediction of optimal quality responses of any potential SRMC product.

Especially, low-repeatability experiments or different values which are appointed to quality criteria created compulsory use of multi-criteria decision making method with fuzzy logic. Slump loss can be seen on concrete in dumping places which has same feature in concrete production plant due to high temperature. Thus slump-spread value may be more important for worker in dumping place than any personnel in concrete plant.

Similarly, concrete which has early strength can be preferred because of conditions based on temperature.

In the modeling of the TOPSIS method, judgments are assigned as crisp numbers in its conventional application. On the other hand, there may be cases in which experts' preferences are uncertain and experts are forced to describe their judgments as uncertain values, such as "between two and four times more important". In such situations, fuzzy version of the TOPSIS method, in which fuzzy numbers instead of crisp ones are used to represent uncertain judgments, is developed and used [22,23].

The argument of our study in literature is not only analyzing the optimal mixture proportion optimization but also researching the development of a mixture dosage prediction model for any possible SRMC product in the future. A prediction model based on ANNs is used for forecasting of appropriate SRMC mixture dosage for any SRMC application in civil engineering environments.

Typically, the ANN model's result contains the optimal factor level's predictions for a possible SRMC application, whereas the FTOPSIS-based Taguchi model's result contains the optimal factor level combination of mixture dosage which can fulfill all multi-response quality characteristics for a specific SRMC application. In the proposed hybrid methodology, the FTOPSIS-based Taguchi model can be used, when an optimization of the factor level combination of mixture dosages for a specific SRMC production is required.

ANN is commonly used to estimate quality criteria as it does not require complex mathematical model based on industrial applications, it has opportunity for easy use and has interface which provides facility of use to user in computer programming languages [28-40]. Contrary to other expert systems, operators who work in companies can use models based on artificial neural nets without requiring complex mathematical formulations and applications.

On the other hand, when a simpler mixture dosage predicting application of any SRMC production is considered as enough, the ANN model can be used. However, the proposed SRMC mix dosage prediction

algorithm, specifically ANN, is expected to reduce the number of experiment and experimental errors, save time, cost, and laborers. The SRMC designed by the proposed algorithm is expected to have lower cement and water contents, higher durability, and better economic effects.

Flow chart of the study which consists of two phases as to be modeling and optimization sections in a standard ready concrete production plant has been given in Section 2. Firstly, incomes which effect on concrete's quality criteria have been determined respectively as amount of cement, water cement ratio, amount of plasticizer, fine aggregate ratio, coarse aggregate ratio, amount of fly ash, mixer mixing time and plasticizer type and experimental design matrix has been determined as considering levels used in company for experimental design (Section 3.1.). On first phase of the study, dosage levels which optimizes parameters of slump-spread value which represents workability feature of concrete, 2-day and 28-days compressive strength value which represent mechanics features, production cost, air content and water absorption percentage (Section 3.1) have been found by FTOPSIS-based Taguchi method (Section 3.2). On this phase, fuzzy method has been used as integrated with experimental design method for the purpose of assessment of all experts' views (Section 3.2).

On the second phase of study, artificial neural nets have been used to estimate concrete quality criteria (Section 3.2). Taguchi based tests have been used to train net to mathematical modeling with artificial neural nets. Then, ten each of tests have been made respectively for test and validation. ANN and fuzzy modeling performance was compared in Section 4.

FTOPSIS and crisp TOPSIS methods have been used on Section 4 in terms of comparing optimization performance. In Section 5, the conclusions are presented.

## 2. The Description of the Structure of the developed Model

Although TOPSIS-based Taguchi Method and ANNs methodologies are explained in the following sections, the readers are referred to 17, 19, 23, 25, 28, 29, 41 and 42 for detailed explanations and application steps of TOPSIS-Taguchi methodology and ANNs.

The developed hybrid model incorporates two separate modules, named 'Multi-Response Optimization

Module: FTOPSIS-Taguchi modeling’ and ‘Prediction Module: ANN modeling’ (Figure 1).

For the first time in this paper, the application of integrating Fuzzy TOPSIS and Taguchi method is applied to solve SRMC mixture optimization problem. In addition to the multi-response Taguchi optimization module, the ANN module used in this study provides prediction of possible optimal mixture proportions of

### 3. Computational Application to Illustrate the Hybrid Multi-response Optimization Algorithm

In this section, the computational application which is proposed to illustrate the performance of the hybrid multi-response optimization algorithm is described. After that, the results obtained are presented and analyzed

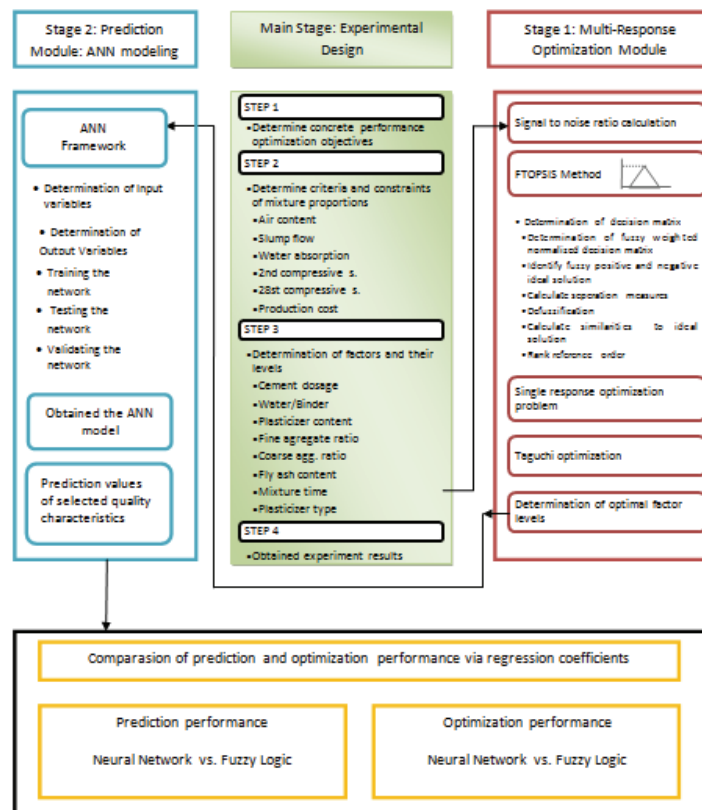


Fig. 1. Proposed performance optimization and modeling framework justified manually.

SRMC for any possible engineering application.

The model which may be designed, gives us the ability to predict a possible SRMC application’s quality responses for a given set of mixture parameters. Similarly, we may seek the variable-setting that minimizes the cost of production. The details of modules and examples are presented in the following sections.

#### 3.1. Experimental Design

##### 3.1.1. Determination of criteria and constraints of mixture dosages

The cement used in this application is a CEM I 42.5 R. Chemical compositions of the binder materials is given in Table 1 and 2 [9]. Table 3 presents the aggregate sieve analysis.

Table 1. Chemical composition of cement and fly ash [19]

Chemical analysis	CEM I 42.5 R (%)	FLY ASH (%)
CaO	66.25	4.76
SiO <sub>2</sub>	21.79	56.21
Al <sub>2</sub> O <sub>3</sub>	5.98	23.1
Fe <sub>2</sub> O <sub>3</sub>	2.51	6.51
SO <sub>3</sub>	1.54	0.73
MgO	1.15	2.11
K <sub>2</sub> O	0.61	2.53
Na <sub>2</sub> O	0.15	0.27
Cl	0.0071	0.0018
Loss of ignition	3.71	2.24

greater than 220 mm, this concrete is considered vibrator-free special concrete according to TS EN 206-1 [43]. If slump flow range is between the range of 10–50 mm this concrete is considered road concrete according to TS EN 206-1 [43].

The air content percentage of standard concrete should be minimized [9]. The unit weight of fresh concrete depends on aggregate granulation, application of squeezing and amount of entrained air. In addition, the

Table 2. Properties of the SPs at 20°C

Properties	Superplasticizers			
	Polycarboxylic type polymer	Polycarboxylic polymer	type	Polycarboxylic polymer
Chemical description	Light Brown	Brown		Brown
Color				
Specific gravity (kg/L)	1.045 – 1.085	1.061 – 1.101		1.059 – 1.099
Chlorin content % (EN 480-10)	< 0.1	< 0.1		< 0.1
Alkaline content% (EN 480-12)	< 3	< 3		< 3
State	Liquid	Liquid		Liquid
Symbol	PCE I	PCE II		PCE III

Table 3. Aggregate sieve analysis [51]

Sieves (mm)	% passing through sieves		
	Crushed sand: particle size smaller than 4 mm (I)	particle size between 4 mm to 11.2 mm (II)	particle size between 11.2 mm to 22.4mm (III)
31.5	100	100	100
22.4	100	100	97.7
16	100	100	41.8
12.5	100	95.7	2.8
8	100	30.8	1.4
4	99.7	2.6	1.4
2	66.4	1.7	1.4
1	40.9	1.5	1.3
0.5	26.3	1.1	0.9
0.25	18.3	1.1	0.9
0.125	11.1	1.1	0.9
0.063	10.8	1.1	0.9
fineness	3.4	6.6	7.5

3.1.2. Determination of concrete performance optimization objectives

The minimum concrete temperature must be 5°C [43]. Slump flow range can be 10–220 mm for Standard Weight concrete [44]. Moreover, if slump flow range is

compressive strengths of three 150 mm cube concrete samples per experiment are determined on the 2th and 28th days according to TS EN 12390/3 [45]. Each compressive strength experiment is an average of the results coming from three 150 mm cube concrete specimens.

The cube compressive strength at 28 days of standard concrete is considered to be in the range of 10.0–60.0 N/mm<sup>2</sup> [43]. Higher compressive strength means better concrete quality. One other criterion is water absorption of concrete mixtures which also should be minimized [9, 43]. The compressive test apparatus is given in Figure 2.

Six quality characteristics are identified for standard concrete. Quality characteristics for optimization phase are presented in Table 4. The basic concepts of triangular fuzzy numbers are given below [22,23, and 45]:



Figure 2. Compressive strength test apparatus

A general definition of a fuzzy number is given by Chen and Hwang [45], as any fuzzy subset  $M = \{x, \mu_M(x)\}$  where  $x$  takes its number on the real line  $R$  and  $\mu_M(x) \in [0,1]$ . This membership function  $\mu_M(x)$  can be determined by the following: *i.* Continuous mapping from  $R$  to the closed interval  $[0,1]$ ; *ii.* Constant on  $(-\infty, a]$ :  $\mu_M(x) = 0, \forall x \in (-\infty, a]$ ; *iii.* Strictly increasing on  $[a,b]$ ; *iv.* Constant on  $[b]$ :  $\mu_M(x) = 1, \forall x \in [b]$ ; *v.* Strictly decreasing on  $[b,c]$ ; *vi.* Constant on  $[c, +\infty)$ :  $\mu_M(x) = 0, \forall x \in [c, +\infty)$ . Hence, a triangular fuzzy number,  $\tilde{A} = (a,b,c), a \leq b \leq c$ , its membership function ( $\mu(x)$ ) is defined by Chen and Hwang [45]:

$$\mu(x) = \begin{cases} 1 & x = b \\ \frac{x-a}{b-a} & a \leq x \leq b \\ \frac{c-x}{c-b} & b \leq x \leq c \\ 0 & \text{other} \end{cases} \quad (1)$$

$\tilde{A} = (a_1, a_2, a_3)$  and  $\tilde{B} = (b_1, b_2, b_3)$  be any two positive triangular fuzzy numbers. Then the arithmetic operations are defined by Chen and Hwang [45]:

$$\tilde{A} \oplus \tilde{B} = [a_1 + b_1, a_2 + b_2, a_3 + b_3] \quad (2)$$

$$\tilde{A} \otimes \tilde{B} = [a_1 \times b_1, a_2 \times b_2, a_3 \times b_3] \quad (3)$$

$$\tilde{A} \oslash \tilde{B} = [a_1 / b_3, a_2 / b_2, a_3 / b_1] \quad (4)$$

For a triangular fuzzy number  $\tilde{A} = (a_1, a_2, a_3)$  its

Table 4. Quality characteristics and their target values for optimization phase

Quality Characteristic	Symbol	Description	Type of concrete test	Target values	Expert evaluation (Individual weighting)			Corresponding Fuzzy Weights <sup>a</sup>	Normalized Fuzzy Weights		
					Expert 1	Expert 2	Expert 3				
1	R1	Air content (%)	Fresh concrete test	Smaller is better	4	5	7	(4 <sup>a</sup> , 5 <sup>b</sup> , 7 <sup>c</sup> )	0.085,	0.119,	0.200
2	R2	Slump flow (cm)	Fresh concrete test	Larger is better	8	8	6	(6, 8, 8)	0.128,	0.190,	0.229
3	R3	Water absorption (%)	Hardened concrete test	Smaller is better	4	5	6	(4, 5, 6)	0.085,	0.119,	0.171
4	R4	Compressive strength (N/mm <sup>2</sup> ) 2 day	Hardened concrete test	Larger is better	9	7	8	(7, 8, 9)	0.149,	0.190,	0.257
5	R5	Compressive strength (N/mm <sup>2</sup> ) 28 days	Hardened concrete test	Larger is better	9	8	9	(8, 9, 9)	0.170,	0.214,	0.257
6	R6	Production Cost (\$/mm <sup>2</sup> )	Fresh concrete test	Smaller is better	6	7	8	(6, 7, 8)	0.128,	0.167,	0.229
<b>Total</b>								<b>(35,42,47)</b>	<b>(0.745,</b>	<b>1.000,</b>	<b>1.343)</b>

<sup>a</sup> The weights of responses are determined by three laboratory expert works in dump areas, quality laboratory and R&D department respectively.

(a,b,c) represents triangular fuzzy number. A triangular fuzzy number (4, 5, 7) corresponds to “about 5 to 1” expression [22, 23, and 45].

defuzzification value is defined to be

$$\tilde{A} = \frac{a_1 + a_2 + a_3}{3} \tag{5}$$

3.1.3. Determination of concrete performance optimization objectives

Seven factors each of which have three levels and one factor that has two levels affect the SRMC identified quality. Cement dosage is determined as a two level factor and water to binder materials ratio, the percentage of super plasticizer content, fine aggregate to total aggregate ratio, coarse aggregate (I) to total aggregate ratio, fly ash dosage, mixture time of fresh concrete and type of SP are identified as three level factors. These factors are symbolized X<sub>1</sub>, X<sub>2</sub>, X<sub>3</sub>, X<sub>4</sub>, X<sub>5</sub>, X<sub>6</sub>, X<sub>7</sub> and X<sub>8</sub> respectively (Table 5). Estimated production cost for experiments are presented in Table 6.

represent the eight mixture dosages (factors) and their levels. Signal to Noise Ratios (SNRs) for smaller the better and larger the better response are calculated by using Eq. (6) and (7) for each response [41].

$$\eta = -10 \log_{10} \left[ \frac{1}{n} \sum_{i=1}^n y_i^2 \right] \tag{6}$$

$$\eta = -10 \log_{10} \left[ \frac{1}{n} \sum_{i=1}^n \frac{1}{y_i^2} \right] \tag{7}$$

where, η is the signal- to- noise ratio and y<sub>i</sub> is the experiment result for the scenario i; n is the total number of replications. Taguchi uses SNRs as a measure of the process sensitivity to noise, allowing the identification of the process variable that may affect variation [47]. A system that is sensitive to noise will have a low SNR. Therefore, to achieve what Taguchi designates as a “robust design”, one must therefore

Table 5. Levels of factors that affect quality characteristics for optimization phase

Factors	Description	Bounds		
		First bound	Second bound	Third bound
X <sub>1</sub>	Cement dosage (kg)	300	<u>350*</u>	
X <sub>2</sub>	Water to binder materials ratio	0.45	<u>0.50*</u>	0.55
X <sub>3</sub>	Super plasticizer content (%)	1.00	1.25	<u>1.50*</u>
X <sub>4</sub>	fine aggregate (I) to total aggregate ratio	<u>0.45*</u>	0.50	0.55
X <sub>5</sub>	coarse aggregate (I) to total aggregate ratio	0.25	<u>0.30*</u>	0.35
X <sub>6</sub>	Fly ash content (kg)	60	80	<u>100</u>
X <sub>7</sub>	Mixture time (s)	100	<u>110</u>	120
X <sub>8</sub>	Type of SP	<u>PCE I</u>	PCE II	PCE III

\* Mixture level using in the ready-mixed concrete plant

3.2. Multi-response optimization module: FTOPSIS-based Taguchi Optimization

3.2.1. Signal to noise ratio calculations

L<sub>18</sub> (2<sub>1</sub>×3<sub>7</sub>) orthogonal array [46] is used to implement the experiments according to Taguchi’s parameter design principles (Figure 3). In Figure 3, columns 2–9

maximize the SNR ratio. The experimental design (L<sub>18</sub>), experimental results (Mean Values) and SNRs are given in Figure 3.

Table 6. Estimated production cost for all experiments (\$/ m<sup>3</sup>)

Exp. No.	Fly ash	Cement	SP amount	Water	Aggregate #1	Aggregate #2	Production Cost
1	1.698	20.4	4.860	0.448125	3.8270	4.0515	35.28463
2	2.264	20.4	6.225	0.4571875	4.1796	3.6260	37.15179
3	2.830	20.4	7.650	0.46625	4.5236	3.2079	39.07775
4	2.264	20.4	4.980	0.5109375	3.6765	3.8924	35.72384
5	2.830	20.4	6.375	0.5215625	4.0119	3.478	37.61646
6	1.698	20.4	7.290	0.495	4.5709	3.2412	37.69510
7	2.830	20.4	5.1	0.5765625	3.913	3.3892	36.20876
8	1.698	20.4	6.075	0.5475	4.4634	3.1635	36.34740
9	2.264	20.4	7.47	0.5590625	3.5862	3.7999	38.07916
10	2.264	23.8	5.73	0.528435	4.3516	3.0858	39.75984
11	2.830	23.8	7.32	0.5371875	3.4959	3.7037	41.68679
12	1.698	23.8	8.415	0.5128125	4.0205	3.4854	41.93171
13	1.698	23.8	5.61	0.575625	3.913	3.3929	38.98953
14	2.264	23.8	7.17	0.5859375	4.2226	2.997	41.03954
15	2.830	23.8	8.775	0.5959375	3.3927	3.5927	42.98634
16	2.830	23.8	5.85	0.6621875	4.0205	2.849	40.01169
17	1.698	23.8	7.02	0.631875	3.4228	3.6223	40.19498
18	2.264	23.8	8.595	0.64375	3.7281	3.2301	42.26095

Exp. No.	Taguchi Design								Responses (Mean Values)						SNR (Signal/Noise Ratio)						Normalized Decision Matrix								
	X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	X <sub>4</sub>	X <sub>5</sub>	X <sub>6</sub>	X <sub>7</sub>	X <sub>8</sub>	R1	R2	R3	R4	R5	R6	R1	R2	R3	R4	R5	R6	R1	R2	R3	R4	R5	R6			
1	1	1	1	1	1	1	1	1	2.0	25	1.688	33.9	54.80	35.284	-6.02060*	27.9588	-4.55147	30.6040	34.7756	-30.9517	-0.398*	0.151	-0.204	0.241	0.239	-0.229			
2	1	1	2	2	2	2	2	2	1.5	45	0.907	36.3	59.80	37.151	-3.52183	33.0643	0.83838	31.1981	35.5340	-31.3996	-0.233	0.178	0.038	0.246	0.244	-0.233			
3	1	1	3	3	3	3	3	3	0.9	70	1.913	36.6	55.00	39.077	0.91515	36.9020	-5.63693	31.2696	34.8073	-31.8386	0.060	0.199	-0.252	0.247	0.239	-0.236			
4	1	2	1	1	2	2	3	3	1.3	130	1.715	28.5	52.55	35.723	-2.27887	42.2789	-4.68876	29.0969	34.4115	-31.0592	-0.150	0.228	-0.210	0.229	0.236	-0.230			
5	1	2	2	2	3	3	1	1	1.8	150	1.712	30.2	52.56	37.616	-5.10545	43.5218	-4.67281	29.6001	34.4131	-31.5076	-0.337	0.235	-0.209	0.233	0.236	-0.233			
6	1	2	3	3	1	1	2	2	1.3	150	2.652	30.3	51.10	37.695	-2.27887	43.5218	-8.47371	29.6289	34.1684	-31.5257	-0.150	0.235	-0.379	0.234	0.235	-0.234			
7	1	3	1	2	1	3	2	3	1.6	190	1.803	23.3	42.69	36.208	-4.08240	45.5751	-5.12175	27.3471	32.6065	-31.1765	-0.270	0.246	-0.229	0.216	0.224	-0.231			
8	1	3	2	3	2	1	3	1	1.2	170	1.980	28.7	49.46	36.347	-1.58362	44.6090	-5.93363	29.1576	33.8851	-31.2095	-0.105	0.241	-0.266	0.230	0.233	-0.231			
9	1	3	3	1	3	2	1	2	1.3	230	1.035	26.0	46.50	38.079	-2.27887	47.2346	-0.29982	28.2995	33.3491	-31.6137	-0.150	0.255	-0.013	0.223	0.229	-0.234			
10	2	1	1	3	3	2	2	1	2.1	60	1.805	39.7	59.20	39.759	-6.44439	35.5630	-5.13386	31.9758	35.4464	-31.9889	-0.426	0.192	-0.230	0.252	0.243	-0.237			
11	2	1	2	1	1	3	3	2	1.4	130	1.610	42.1	61.60	41.686	-2.92256	42.2789	-4.13827	32.4856	35.7916	-32.4000	-0.193	0.228	-0.183	0.256	0.246	-0.240			
12	2	1	3	2	2	1	1	3	0.8	150	1.817	36.4	61.23	41.931	1.93820	43.5218	-5.18734	31.2220	35.7393	-32.4509	0.128	0.235	-0.232	0.246	0.245	-0.240			
13	2	2	1	2	3	1	3	2	1.2	210	2.079	31.1	54.09	38.989	-1.58362	46.4444	-6.35874	29.8552	34.6623	-31.8190	-0.105	0.251	-0.285	0.235	0.238	-0.236			
14	2	2	2	3	1	2	1	3	0.8	230	2.042	31.4	50.80	41.039	1.93820	47.2346	-6.20369	29.9386	34.1173	-32.2640	0.128	0.255	-0.278	0.236	0.234	-0.239			
15	2	2	3	1	2	3	2	1	1.5	250	1.478	33.9	50.58	42.986	-3.52183	47.9588	-3.39730	30.6040	34.0796	-32.6666	-0.233	0.259	-0.152	0.241	0.234	-0.242			
16	2	3	1	3	2	3	1	2	1.1	280	2.066	26.3	42.38	40.011	-0.82785	48.9432	-6.30577	28.3991	32.5432	-32.0437	-0.055	0.264	-0.282	0.224	0.223	-0.237			
17	2	3	2	1	3	1	2	3	0.7	290	1.912	28.7	49.56	40.195	3.09804	49.2480	-5.63203	29.1576	33.9026	-32.0834	0.205	0.266	-0.252	0.230	0.233	-0.238			
18	2	3	3	2	1	2	3	1	0.5	420	2.001	24.0	48.23	42.260	6.02060	52.4650	-6.02610	27.6042	33.6663	-32.5188	0.398	0.283	-0.270	0.218	0.231	-0.241			
The square root of sum of squares of each element in the columns															15.14*	185.3	22.34	126.8	145.7	134.96									

\* (-6.02060/15.14)=-0.398

Figure 3. Findings were obtained in all experiments by Taguchi experiments



3.2.2. Fuzzy TOPSIS methodology

In Figure 3, columns 16-21 are illustrated as decision matrix for the first step of the FTOPSIS method [22, 23, 45, and 49]. The normalized and then the fuzzy weighted normalized decision matrix are obtained

respectively (Figure 3 and 4). The positive (A\*) and negative ideal solutions (A-) (see Figure 4) and the separation measures (d<sub>i</sub><sup>+</sup> and d<sub>i</sub><sup>-</sup>) (see Figure 5) are also determined. Finally, the final ranking scores of each scenario (C<sub>i</sub><sup>\*</sup>) are calculated by using the FTOPSIS procedure [22, 23 and see also 45] (Figure 5).

Exp. No	Weighted normalized fuzzy decision matrix																	
	(0.085, 0.119, 0.2) *			(0.128, 0.19, 0.229) *			(0.085, 0.119, 0.171) *			(0.149, 0.19, 0.257) *			(0.17, 0.214, 0.257) *			(0.128, 0.167, 0.229) *		
	v <sub>R1</sub>			v <sub>R2</sub>			v <sub>R3</sub>			v <sub>R4</sub>			v <sub>R5</sub>			v <sub>R6</sub>		
1	-0.03*	-0.05*	-0.080*	0.019	0.029	0.034	-0.017	-0.024	-0.035	0.036	0.046	0.062	0.041	0.051	0.061	-0.029	-0.038	-0.052
2	-0.02	-0.03	-0.047	0.023	0.034	0.041	0.003	0.004	0.006	0.037	0.047	0.063	0.042	0.052	0.063	-0.030	-0.039	-0.053
3	0.01	0.01	0.012	0.025	0.038	0.046	-0.021	-0.030	-0.043	0.037	0.047	0.063	0.041	0.051	0.061	-0.030	-0.039	-0.054
4	-0.01	-0.02	-0.030	0.029	0.043	0.052	-0.018	-0.025	-0.036	0.034	0.044	0.059	0.040	0.051	0.061	-0.029	-0.038	-0.053
5	-0.03	-0.04	-0.067	0.030	0.045	0.054	-0.018	-0.025	-0.036	0.035	0.044	0.060	0.040	0.051	0.061	-0.030	-0.039	-0.053
6	-0.01	-0.02	-0.030	0.030	0.045	0.054	-0.032	-0.045	-0.065	0.035	0.045	0.060	0.040	0.050	0.060	-0.030	-0.039	-0.053
7	-0.02	-0.03	-0.054	0.031	0.047	0.056	-0.020	-0.027	-0.039	0.032	0.041	0.055	0.038	0.048	0.058	-0.029	-0.039	-0.053
8	-0.01	-0.01	-0.021	0.031	0.046	0.055	-0.023	-0.032	-0.046	0.034	0.044	0.059	0.040	0.050	0.060	-0.030	-0.039	-0.053
9	-0.01	-0.02	-0.030	0.033	0.049	0.058	-0.001	-0.002	-0.002	0.033	0.043	0.057	0.039	0.049	0.059	-0.030	-0.039	-0.054
10	-0.04	-0.05	-0.085	0.025	0.037	0.044	-0.020	-0.027	-0.039	0.038	0.048	0.065	0.041	0.052	0.063	-0.030	-0.040	-0.054
11	-0.02	-0.02	-0.039	0.029	0.043	0.052	-0.016	-0.022	-0.032	0.038	0.049	0.066	0.042	0.053	0.063	-0.031	-0.040	-0.055
12	0.01	0.02	0.026	0.030	0.045	0.054	-0.020	-0.028	-0.040	0.037	0.047	0.063	0.042	0.053	0.063	-0.031	-0.040	-0.055
13	-0.01	-0.01	-0.021	0.032	0.048	0.057	-0.024	-0.034	-0.049	0.035	0.045	0.061	0.040	0.051	0.061	-0.030	-0.039	-0.054
14	0.01	0.02	0.026	0.033	0.049	0.058	-0.024	-0.033	-0.048	0.035	0.045	0.061	0.040	0.050	0.060	-0.031	-0.040	-0.055
15	-0.02	-0.03	-0.047	0.033	0.049	0.059	-0.013	-0.018	-0.026	0.036	0.046	0.062	0.040	0.050	0.060	-0.031	-0.040	-0.055
16	0.00	-0.01	-0.011	0.034	0.050	0.060	-0.024	-0.034	-0.048	0.033	0.043	0.058	0.038	0.048	0.057	-0.030	-0.040	-0.054
17	0.02	0.02	0.041	0.034	0.051	0.061	-0.021	-0.030	-0.043	0.034	0.044	0.059	0.040	0.050	0.060	-0.030	-0.040	-0.054
18	0.03	0.05	0.080	0.036	0.054	0.065	-0.023	-0.032	-0.046	0.032	0.041	0.056	0.039	0.050	0.059	-0.031	-0.040	-0.055
A*(Max.)	0.03	0.05	0.080	0.036	0.054	0.065	0.003	0.004	0.006	0.038	0.049	0.066	0.042	0.053	0.063	-0.029	-0.038	-0.052
A-(Min.)	-0.04	-0.05	-0.085	0.019	0.029	0.034	-0.032	-0.045	-0.065	0.032	0.041	0.055	0.038	0.048	0.057	-0.031	-0.040	-0.055

\* Triangular fuzzy weights  
 \* 0.398\*0.085=0.03  
 \* 0.398\*0.119=0.05  
 \* 0.398\*0.2=0.08

Figure 4. Fuzzy TOPSIS application: Weighted normalized decision matrix and defuzzification results

Exp. No.	The distance from an alternative i to the ideal solution	The distance from an alternative i to the negative ideal solution	FTOPSIS ranking scores
	d <sub>i</sub> <sup>+</sup>	d <sub>i</sub> <sup>-</sup>	C <sub>i</sub> <sup>*</sup>
1	0.174*	0.038*	0.178*
2	0.113	0.099	0.468
3	0.106	0.106	0.499
4	0.129	0.084	0.394
5	0.154	0.058	0.276
6	0.149	0.063	0.295
7	0.150	0.062	0.291
8	0.128	0.084	0.398
9	0.102	0.111	0.521
10	0.172	0.040	0.188
11	0.126	0.086	0.407
12	0.087	0.125	0.591
13	0.127	0.085	0.402
14	0.093	0.119	0.561
15	0.127	0.085	0.400
16	0.123	0.089	0.421
17	0.078	0.134	0.631
18	0.053	0.159	0.750

\*  $\frac{1}{3} * [(-0.03-0.03)^2 + (-0.05-0.05)^2 + (-0.08-0.08)^2]^{1/2} = 0.174$   
 \*  $\frac{1}{3} * [(0.019-0.036)^2 + (0.029-0.054)^2 + (0.034-0.065)^2]^{1/2} = 0.038$   
 \*  $\frac{1}{3} * [(-0.017-0.003)^2 + (-0.024-0.004)^2 + (-0.035-0.006)^2]^{1/2} = 0.113$   
 \*  $\frac{1}{3} * [(0.036-0.038)^2 + (0.046-0.049)^2 + (0.062-0.060)^2]^{1/2} = 0.106$   
 \*  $\frac{1}{3} * [(0.041-0.042)^2 + (0.051-0.053)^2 + (0.061-0.063)^2]^{1/2} = 0.129$   
 \*  $\frac{1}{3} * [(-0.029-0.029)^2 + (-0.038-0.038)^2 + (-0.052-0.052)^2]^{1/2} = 0.154$   
 \*  $\frac{1}{3} * [(-0.03-0.04)^2 + (-0.05-0.05)^2 + (-0.08-0.085)^2]^{1/2} = 0.149$   
 \*  $\frac{1}{3} * [(0.019-0.019)^2 + (0.029-0.029)^2 + (0.034-0.034)^2]^{1/2} = 0.150$   
 \*  $\frac{1}{3} * [(-0.017-0.032)^2 + (-0.024-0.045)^2 + (-0.035-0.065)^2]^{1/2} = 0.128$   
 \*  $\frac{1}{3} * [(0.036-0.032)^2 + (0.046-0.041)^2 + (0.062-0.065)^2]^{1/2} = 0.102$   
 \*  $\frac{1}{3} * [(-0.041-0.038)^2 + (-0.051-0.048)^2 + (-0.061-0.057)^2]^{1/2} = 0.172$   
 \*  $\frac{1}{3} * [(-0.029-0.031)^2 + (-0.038-0.040)^2 + (-0.052-0.055)^2]^{1/2} = 0.126$   
 \*  $\frac{1}{3} * [(0.038-0.038)^2 + (0.048-0.048)^2 + (0.057-0.057)^2]^{1/2} = 0.087$   
 \*  $\frac{1}{3} * [(0.019-0.019)^2 + (0.029-0.029)^2 + (0.034-0.034)^2]^{1/2} = 0.102$   
 \*  $\frac{1}{3} * [(0.036-0.032)^2 + (0.046-0.041)^2 + (0.062-0.065)^2]^{1/2} = 0.172$   
 \*  $\frac{1}{3} * [(-0.041-0.038)^2 + (-0.051-0.048)^2 + (-0.061-0.057)^2]^{1/2} = 0.126$   
 \*  $\frac{1}{3} * [(-0.029-0.031)^2 + (-0.038-0.040)^2 + (-0.052-0.055)^2]^{1/2} = 0.087$   
 \*  $\frac{1}{3} * [(0.038-0.038)^2 + (0.048-0.048)^2 + (0.057-0.057)^2]^{1/2} = 0.102$

Figure 5. Fuzzy TOPSIS Results

3.2.3. Single-response Taguchi optimization: Determination of optimal factor levels

The average responses by factor levels can be established by using the Taguchi's principles [See Refs

1, 2]. Their associated factor effect plots are given in Figure 6. Taguchi's method results led to the final factor design of (X1)<sub>2</sub> (X2)<sub>3</sub> (X3)<sub>3</sub>(X4)<sub>2</sub> (X5)<sub>2</sub> (X6)<sub>2</sub> (X7)<sub>3</sub> (X8)<sub>3</sub> (Table 7). Experimental results derived from optimum condition and significant anticipated

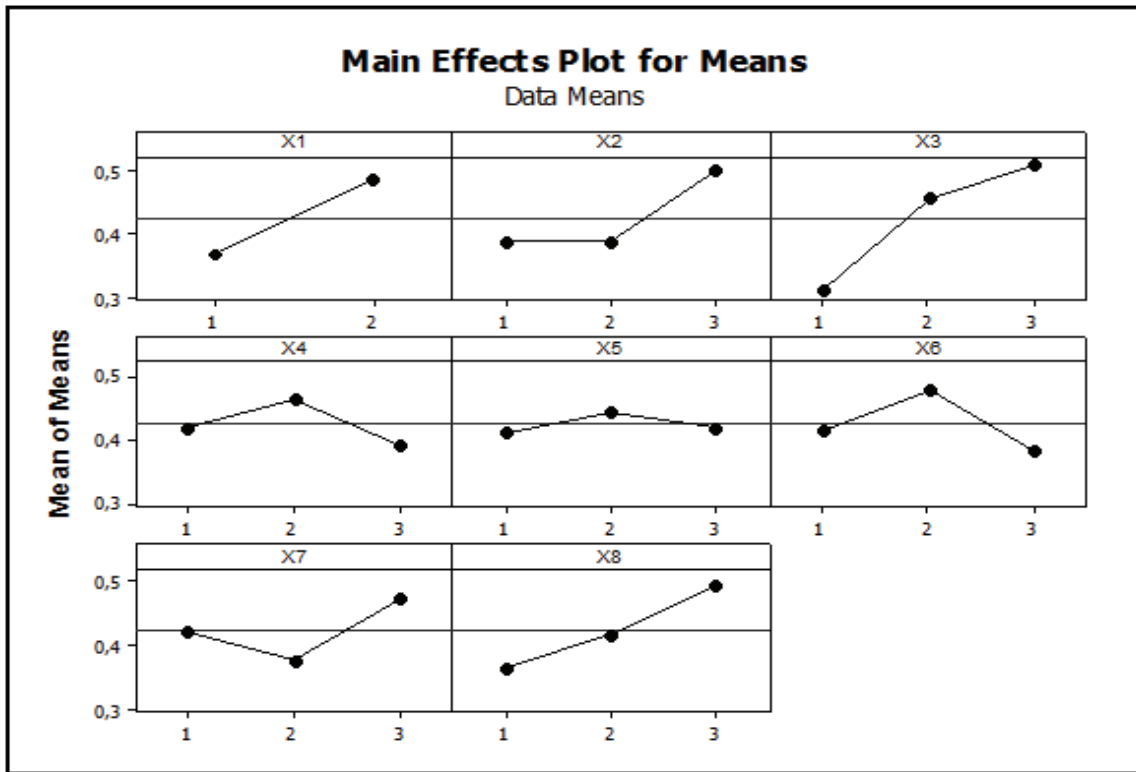


Figure 6. Means plots for factor effects

Table 7. Optimum factors' levels

Factors	X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	X <sub>4</sub>	X <sub>5</sub>	X <sub>6</sub>	X <sub>7</sub>	X <sub>8</sub>
Level 1	0.3689	0.3885	0.3122	0.4220	0.4136	0.4158	0.4245	0.3647
Level 2	<b>0.4834</b>	0.3879	0.4568	<b>0.4628</b>	<b>0.4454</b>	<b>0.4802</b>	0.3789	0.4192
Level 3		<b>0.5020</b>	<b>0.5094</b>	0.3936	0.4194	0.3824	<b>0.4750</b>	<b>0.4944</b>
Optimal factor levels	2	3	3	2	2	2	3	3

Table 8. Anticipated improvement in optimum condition

Responses	Description	Estimated mixture levels before Taguchi experiments (X1) <sub>2</sub> (X2) <sub>2</sub> (X3) <sub>3</sub> (X4) <sub>1</sub> (X5) <sub>2</sub> (X6) <sub>3</sub> (X7) <sub>2</sub> (X8) <sub>1</sub>	Optimal mixture levels after Taguchi experiments (X1) <sub>2</sub> (X2) <sub>3</sub> (X3) <sub>3</sub> (X4) <sub>2</sub> (X5) <sub>2</sub> (X6) <sub>2</sub> (X7) <sub>3</sub> (X8) <sub>3</sub>	Anticipated improvement (dB)	Anticipated improvement (%)
1	Air content (%)	1.5	1.5	0.0	0.0
2	Slump flow (cm)	250	290	0.16	16.0
3	Water absorption (%)	1.48	1.48	0.0	0.0
4	Compressive strength (N/mm <sup>2</sup> ) 2 day	33.9	36.2	2.3	6.7
5	Compressive strength (N/mm <sup>2</sup> ) 28 days	50.58	53.86	3.28	6.5
6	Production Cost (\$/mm <sup>2</sup> )	42.9863	42.25634	0.72996	1.7

Table 9. Validation experiment in optimum condition

Exp. run	<i>L</i> <sub>18</sub> Taguchi design								Responses					
	X1	X2	X3	X4	X5	X6	X7	X8	R1 %	R2 mm	R3 %	R4 (N/mm <sup>2</sup> )	R5 (N/mm <sup>2</sup> )	R6 \$/mm <sup>2</sup>
1	2	3	3	2	2	2	3	3	1.5	290	1.48	36.2	53.86	42.25634

improvement in the FTOPSIS-Taguchi method is given in Table 8.

The verification study results show that proposed results satisfy the expected increase for compressive strength and slump flow and expected decrease for production cost, air content and water absorption (Table 9).

### 3.3. Prediction module: ANN modeling

In this module, a prediction model is developed by using ANN to predict effect of factors (mixture dosages) on the selected quality characteristics of SRMC for any potential application. Slump flow (R2), the 2th day compressive strength (R4), the 28<sup>th</sup> day compressive

strength (R5) and production cost (R6) are the selected quality characteristics for the representative modeling application. The developed neural network in our application has eight parameters in input layer and four responses in output layer. The considered network parameters are as follows: hidden layers: 0, 1, 2; hidden units: 5, 10 and 15; learning cycles = 100, 300 and 500. The data used for training, validating, and calibrating of ANNs are collected from the experiment. The range of the parameters used as input and output variables are presented in Table 5 and Table 10 respectively. A data set including 38 samples determined from experimental results are used for training, testing and validation stages of the ANN model.

The available data set are divided into three groups as training, testing and validation data subsets which consist of 18, 10 and 10 data samples, respectively [25]. Taguchi experimental results are used for training of

network models. Multiple-input neuron models can approximate any linear function (Taguchi experiments are used for training the network) providing a sufficient amount of hidden layer neurons is available. Therefore,

Table 10. The range of the parameters used as output variables

Quality Characteristic	Symbol	Description	Data used in ANN model	
			Minimum	Maximum
2	R2	Slump flow (cm)	1	50
4	R4	Compressive strength (N/mm <sup>2</sup> ) 2 day	20	45
5	R5	Compressive strength (N/mm <sup>2</sup> ) 28 days	40	65
6	R6	Production cost (\$/mm <sup>2</sup> )	35	43.5

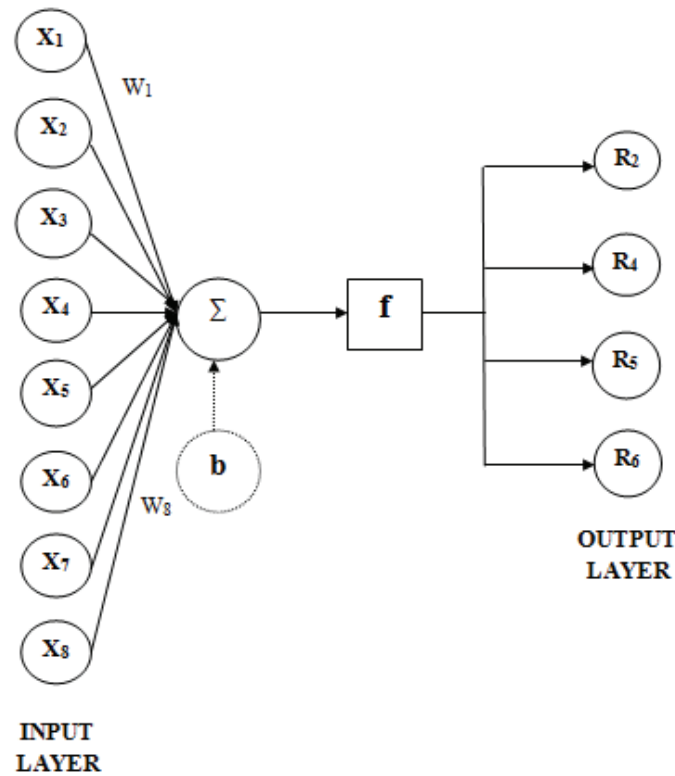


Figure 7. The system used in the ANN model

network models. Moreover, 10 experiments are used for testing and 10 experiments are used for validation of the

multiple-input neuron models are used in this research. The chosen model architecture is shown in Figure 7.

The parameters used in the chosen network can be determined as follows; multiple-input neuron model, adopted in this research, has 8 neurons (variables) in the input layer and 4 neurons in output layer. The computer

Table 11. R<sup>2</sup> results using the ANN model (training phase)

Exp.no.	*R2	‡R2	*R4	‡R4	*R5	‡R5	*R6	‡R6
1	25	14.722	33.9	34.7389	54.80	57.5742	35.28463	35.1892
2	45	37.222	36.3	36.0889	59.80	57.6742	37.15179	37.0857
3	70	59.722	36.6	37.4389	55.00	57.7742	39.07775	38.9822
4	130	109.72	28.5	30.1722	52.55	52.4717	35.72384	35.7712
5	150	119.72	30.2	31.1972	52.56	50.1567	37.61646	37.4069
6	150	157.22	30.3	29.8972	51.10	52.1917	37.69510	37.8819
7	190	205.56	23.3	23.5972	42.69	42.7850	36.20876	36.3266
8	170	213.06	28.7	25.4972	49.46	47.4925	36.34740	36.2071
9	230	243.06	26.0	25.1722	46.50	46.3400	38.07916	38.3293
10	60	83.611	39.7	38.9806	59.20	58.8178	39.75984	39.2338
11	130	163.61	42.1	38.5306	61.60	58.9078	41.68679	41.7508
12	150	151.11	36.4	38.3556	61.23	59.7003	41.93171	41.8311
13	210	181.11	31.1	33.1556	54.09	55.4786	38.98953	38.7452
14	230	221.11	31.4	30.9806	50.80	50.4911	41.03954	40.9755
15	250	271.11	33.9	33.7306	50.58	53.2536	42.98634	42.8980
16	280	277.78	26.3	26.2889	42.38	43.4511	40.01169	39.8857
17	290	305.28	28.7	26.8389	49.56	49.3211	40.19498	40.2527
18	420	365.28	24.0	27.7389	48.23	48.2832	42.26095	42.2832
R <sup>2</sup>	93.9		88.3		90.7		99.5	
	93.5 <sup>†</sup>		87.6 <sup>†</sup>		90.2 <sup>†</sup>		99.4 <sup>†</sup>	

\*Observed results for response  
 ‡Predicted values for response using ANN  
 †R<sup>2</sup> (adj.)

Table 12. R<sup>2</sup> results using the ANN model (testing phase)

Exp. no.	Experiment Runs: coded variables								*R2	‡R2	*R4	‡R4	*R5	‡R5	*R6	‡R6
	X1	X2	X3	X4	X5	X6	X7	X8								
1	2	1	1	1	2	1	3	3	110	107.36	37.8	37.76	61.3	61.29	39.21	39.09
2	2	1	2	1	2	1	2	3	130	133.19	37.6	37.56	60.8	60.82	40.53	40.51
3	2	1	3	2	1	2	1	3	170	168.61	37.1	37.02	57.8	57.77	42.49	42.55
4	2	1	3	2	1	3	2	3	180	180.28	37.9	37.86	57.5	57.54	43.10	43.15
5	2	1	1	2	1	2	3	3	120	116.94	37.5	37.42	58.7	58.72	39.84	39.73
6	1	3	1	3	1	2	1	3	190	185.97	22.8	22.75	42.4	42.38	35.55	35.64
7	1	2	2	2	1	1	3	3	140	138.06	29.7	29.65	53.1	53.06	36.47	36.63
8	1	1	2	2	3	3	3	3	50	36.39	37.1	37.08	57.8	57.83	37.73	37.65
9	1	3	3	3	1	1	1	3	240	242.22	23.2	23.21	44.8	44.82	37.63	37.88
10	1	2	2	1	3	1	2	3	120	118.06	30.3	30.31	53.9	53.92	36.38	36.47
R <sup>2</sup>									99.6		100.0		100.0		99.8	
									99.6 <sup>†</sup>		100.0 <sup>†</sup>		100.0 <sup>†</sup>		99.8 <sup>†</sup>	

\*Observed results for response  
 ‡Predicted values for response using ANN  
 †R<sup>2</sup> (adj.)

program, used in running the network models, is written in MATLAB®. To compare the predicted results obtained from ANN, it transforms them back to their original results and then the mean absolute relative error (MARE) and MSE are gained. The hyperbolic tangent, logarithmic sigmoid and pure linear transfer functions are tried as activation operations for output layer neurons to get the best ANN model [25].

The relationship between prediction results with ANN and experimental results for all concrete criteria is given in Table 11. Validation experiments are also applied at estimated condition. The results demonstrate that the experimental results are close to the estimated results (Tables 12-14).

Table 13. R<sup>2</sup> results using the ANN model (validation phase)

Exp. no.	Experiment Runs: coded variables								*R2	‡R2	*R4	‡R4	*R5	‡R5	*R6	‡R6
	X1	X2	X3	X4	X5	X6	X7	X8								
1	2	2	1	2	1	1	2	3	200	196,94	31,0	30,91	52,9	52,89	39,08	39,05
2	2	2	2	2	1	2	1	3	230	229,03	31,0	30,99	51,1	51,13	41,01	41,06
3	2	2	3	2	1	3	3	3	280	277,36	32,8	32,76	52,5	52,53	42,96	43,10
4	2	2	2	3	1	2	1	3	220	221,11	31,0	30,98	50,5	50,49	41,00	40,98
5	2	2	1	3	1	2	2	3	190	195,28	31,2	31,18	51,0	50,97	39,68	39,56
6	2	3	1	2	1	1	2	3	280	288,61	25,3	25,25	46,8	46,82	38,93	38,99
7	2	3	2	2	1	2	3	3	400	331,53	26,5	26,46	47,2	47,17	40,88	41,02
8	2	3	3	3	1	2	3	3	430	354,86	26,9	26,81	47,1	47,11	42,21	42,35
9	2	3	2	3	1	3	1	3	380	319,03	25,6	25,59	43,1	43,14	41,45	41,51
10	1	3	2	1	3	1	2	3	210	209,72	24,6	24,64	47,9	47,85	36,23	36,40
R <sup>2</sup>									95.7		99.9		99.9		99.8	
									95.1†		99.9†		99.9†		99.7†	

\*Observed results for response

‡Predicted values for response using ANN

†R<sup>2</sup> (adj.)

Table 14. The weights and biases for ANN models\* (in coded values)

Symbol	Weights (w <sub>i</sub> )									Bias (b)
R2	1.9	1833.3	125.0	-158.3	-225	0.3	0.5	-0.0012		-1452.8
R4	0.0	-113.3	1.5	-0.2	12.2	0.0	0.1	-0.0005		62.072
R5	0.0	-121.3	2.3	-12.7	12.8	-0.1	0.1	-0.0002		97.156
R6	0.1	-1.3	5.7	-1.7	-2.4	0.0	0.0	0.0001		6.3898

\*ANNs are composed of numerous of interconnected nonlinear memory less processing elements called neurons.

The neurons of each layer are connected to that of the next layer through associated weights.

The network employs the information of these weights to solve problems. A connected neuron formula is shown as [49]:

$$x = b + \sum_{i=1}^p w_i x_i$$

where b is the bias of neurons. p is the number of elements and w<sub>i</sub> is the weight of the input vector x<sub>i</sub>.

#### 4. Discussion

Artificial neural network are preferred much more in comparison with other data mining and artificial intelligence techniques due to their power, activeness and easy use [50]. Modeling success of artificial neural network method which is preferred on this study due to this feature has been compared with fuzzy logic method which is commonly used. Artificial neural network and fuzzy logic have been preferred as they have easy use and opportunity on tools such as MATLAB®. Moreover, TOPSIS method has been used with fuzzy version on optimization phase. Especially that those experts appoint different weight values to quality criteria causes to be different optimum point found. In order to remove this problem, fuzzy TOPSIS method has been preferred. The data set used for optimizing the criteria was utilized for modeling the concrete quality criteria. The primary purpose is that after the optimization process, we aim to see whether there will be sufficient experimental design based data set for a successful modeling work or not. If the regression coefficient were sufficient, additional experiments causing loss of time and money will not be needed in industry. Also, we had an opportunity to compare modeling and optimization performance with existing methods.

##### 4.1. Prediction performance of ANN and Fuzzy Model

Mamdani fuzzy inference system was used in this study for modeling the quality criteria of standard concrete. In the proposed method, the factors defining the concrete

quality criteria are treated as fuzzy variables. In the modeling of concrete quality criteria under variables such as cement dosage, water to binder ratio, the percentage of super plasticizer content, fine aggregate to total aggregate ratio, coarse aggregate (I) to total aggregate ratio, fly ash dosage, mixture time of fresh concrete are divided into a number of subsets with simple trapezoidal fuzzy membership functions taking into account factors' levels in Taguchi experiments. Membership functions chosen for cement dosage  $X_1$  (normal, high), water to binder ratio  $X_2$ , the percentage of super plasticizer content  $X_3$ , fine aggregate to total aggregate ratio  $X_4$ , coarse aggregate (I) to total aggregate ratio  $X_5$ , fly ash dosage  $X_6$  (low, normal, high) and mixture time of fresh concrete  $X_7$  (short, middle, long) were given in Figure 8, respectively. Membership functions chosen for slump flow according to TSE EN 206-1 [42]; slump (very low, low, normal, high, very high), 2th day compressive strength R4; (bad, poor, normal, good and very good), 28th day compressive strength R5 according to TSE EN 206-1 [42]; (very low, low, normal, high and very high) and production cost R6; (low, normal) were also seen in Figure 8, respectively. In brief, fuzzy inference system model could be seen as schematically in Figure 8.

In this part of study, the developed fuzzy logic-based model was applied to predict the quality characteristics of SC data obtained from Taguchi experiments. The fuzzy rules were written for this purpose. It can be seen from Figure 4 that we devised the fuzzy logic-based algorithm model by using the FL toolbox in MATLAB®. The FL model had seven input parameters and four output parameters.

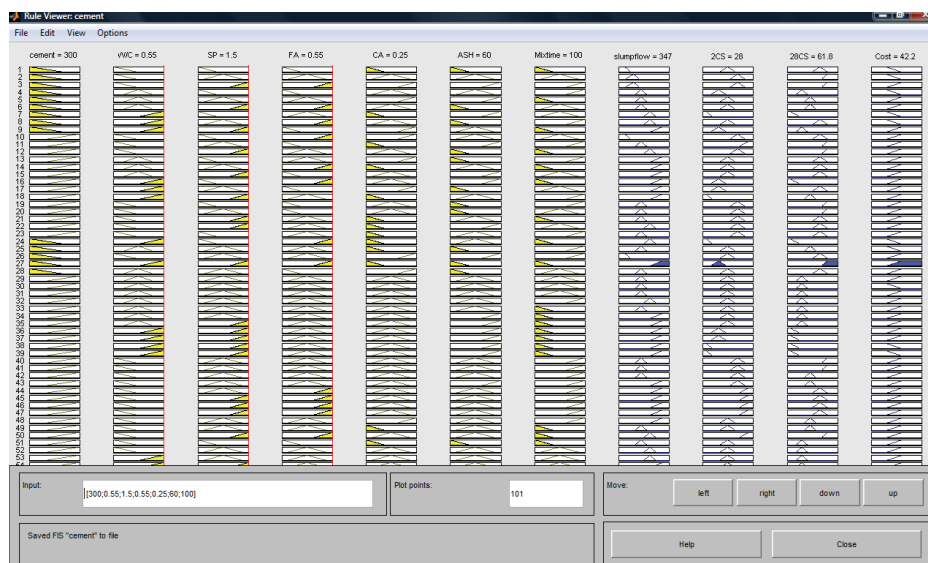


Figure 8. Rule viewer used for fuzzy modeling (validation experiment no: 9)

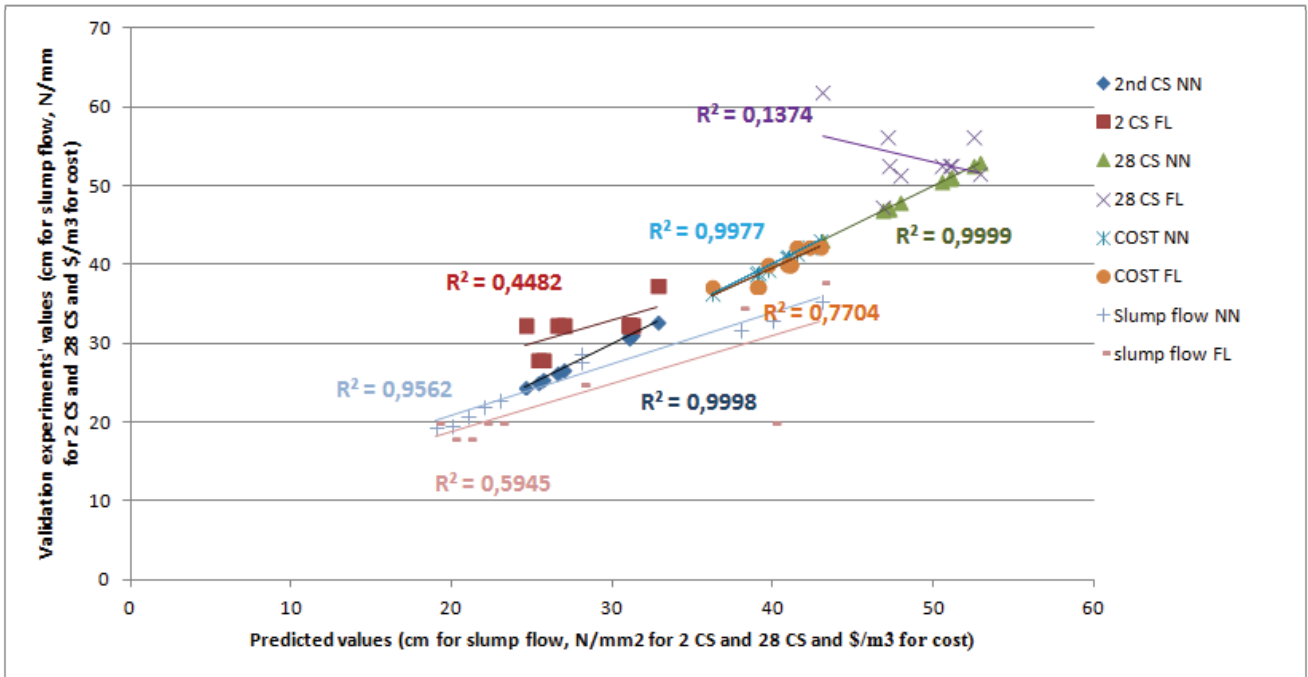


Figure 9. Experimental values vs. predicted values for validation data in Table 13 using fuzzy logic (FL) and neural network (NN)

When fuzzy logic is compared with modeling performance of artificial neural nets, it is seen that artificial neural nets exhibit less data set and more successful estimation performance (Figure 9). For example, when regression coefficients are compared on modeling with artificial neural nets against modeling with fuzzy logic; value 0.96 has been gotten against

twenty eight-day compressive strength and value 0.99 has been obtained against value 0.77 on production cost.

#### 4.2. Optimization performance of TOPSIS and Fuzzy TOPSIS

It can be seen in Figure 10 that in the results of the

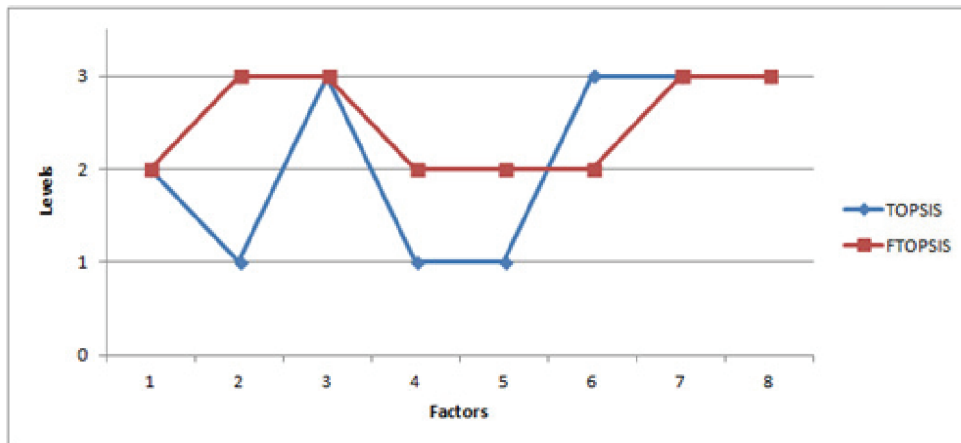


Figure 10. Optimum factor levels obtained by TOPSIS and FTOPSIS

slump-spread value 0.59, value 0.99 has been obtained against value 0.45 on two - day compressive strength, value 0.99 has been obtained against value 0.14 on

TOPSIS based Taguchi optimization model, the optimal factor levels are dissimilar to those derived by the result of the FTOPSIS-based Taguchi approach. Optimal



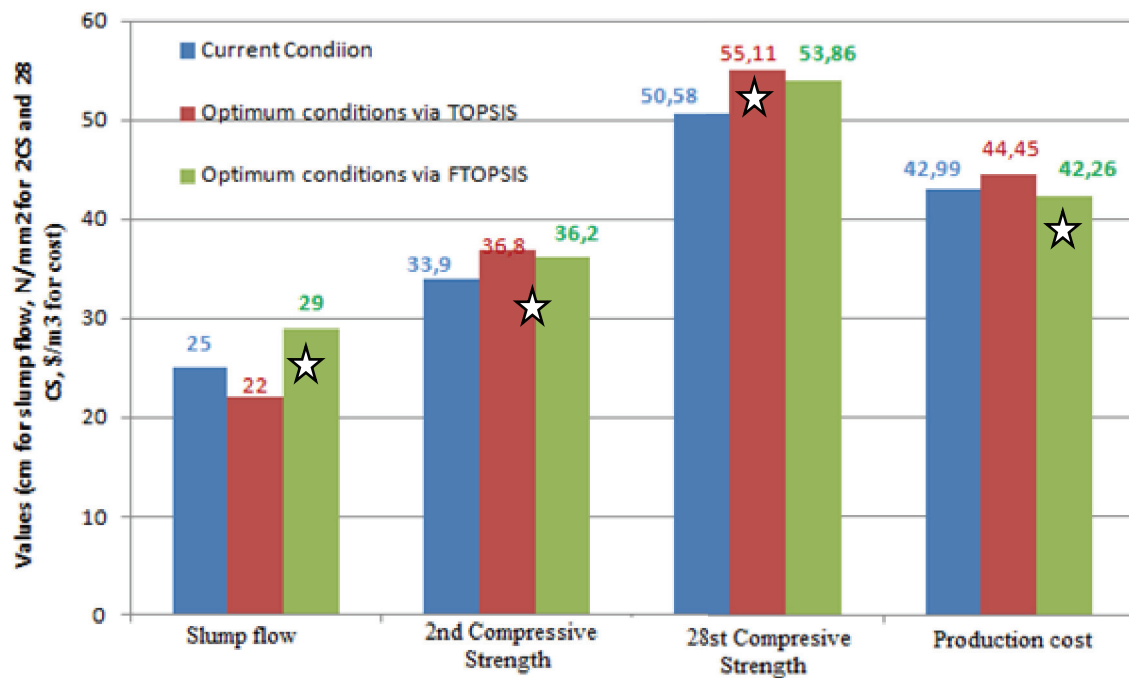


Figure 11. Optimum values for Topsis vs. FTopsis

dosage levels which are gotten by Topsis based Taguchi optimization application which is made in consideration with weights that only a single expert gives them (details of method can be found in [19]) are different from optimal dosage levels which are gotten on FTopsis based Taguchi optimization application that is made in consideration with weights that all experts give to quality criteria.

The results show that FTopsis based Taguchi optimization is more effective than Topsis based Taguchi optimization according to production cost. 5.1% less cost and same quality concrete has been produced by FTopsis based Taguchi method than Topsis based Taguchi method on production cost (Figure 11). Differences among ambient conditions in concrete production plant and concrete dumping places cause that they assign concrete technician to different level of significance for different quality criteria. Concrete slump loss is seen due to temperature on production and casting points, so concrete's slump-spread value is more important for worked in dumping place.

### 5. Conclusions

In this study, the hybrid optimization and the modeling of mixture proportions of standard concrete (SRMC) are carried out by using the Fuzzy Topsis (FTopsis)-Taguchi model and artificial neural networks (ANNs). The developed model incorporates two separate modules, named ‘Multi-Response Optimization: FTopsis-Taguchi modeling’ and ‘Prediction: ANN modeling’.

Multi-response optimization module is used in this study to examine the ranking of the conflicting mixture dosage factors’ levels and the best possible mix proportions of SRMC. On the other hand the prediction model of possible mixture dosage combination levels of any possible SRMC production process are built based on ANNs. ANN-based model puts forward successful prediction results. The high correlation in ANN model for slump flow, the 2th day and 28th day compressive strength and production cost responses (Table 11, 12 and 13) indicates that the ANN model can be used as a more accurate tool to model the concrete quality (Figure 9). The concrete manufacturing which has similar

mechanical properties was provided with lower cost by FTOPSIS method (Figure 11). The results show the efficiency and effectiveness of the proposed method.

This study represents an experimental study of mixture dosage optimization for the standard ready-mixed concrete sector. The optimal mixture dosage levels are selected considering not only the required quality characteristics of SRMC but also economic aspects which are lacking in many applications but are very important to be competitive in this sector.

## References

1. S. Yan, H.C. Lin, Y.C. Liu, Optimal schedule adjustments for supplying ready mixed concrete following incidents, *Automation in Construction*, 20 (2011), 1041–1050.
2. C.Y. Chang, R. Huang, P.C. Lee, T.L. Weng, Application of a weighted Grey-Taguchi method for optimizing recycled aggregate concrete mixtures, *Cement and Concrete Composites*, 33 (2011), 1038–1049.
3. O. Akalin, K.O. Okay, B. Sennaroğlu, M. Tez, Optimization of chemical admixture for concrete on mortar performance tests using mixture experiments. *Chemometrics and Intelligent Laboratory Systems* 104 (2010), 233–242.
4. S. Hinişoğlu, O.U. Bayrak, Optimization of early flexural strength of pavement concrete with silica fume and fly ash by the Taguchi method. *Civil Engineering and Environmental Systems* 1 (2) (2010), 79–90.
5. M. Muthukumar, D. Mohan, Optimization of mechanical properties of polymer concrete and mix design recommendation based on design of experiments, *Journal of Applied Polymer Science*, 94 (2004), 1107–17.
6. O. Tan, A.S. Zaimoğlu, S. Hinişoğlu, S. Altun, Taguchi approach for optimization of the bleeding on cement-based grouts, *Tunnelling Underground Space Technology*, 20 (2) (2005), 167–73.
7. I. Türkmen, R. Gül, C. Çelik, A Taguchi approach for investigation of some physical properties of concrete produced from mineral admixtures, *Building and Environment*, 43 (2008), 1127–1137.
8. K.T. Fauzan, M. Hosino, A. Morita, The influence of mixing techniques on the properties of concrete by using air entraining agent and high range water reducer agent. *Jurnal Itenas* 7 (3) (2003) 1–10.
9. E. Özbay, A. Öztaş, A. Baykaşoğlu, H. Özbebek, Investigating mix proportions of high strength self-compacting concrete by using Taguchi method, *Construction and Building Materials*, 23 (2009), 694–702.
10. M. Olivia, H. Nikraz, Properties of fly ash geopolymer concrete designed by Taguchi method, *Materials & Design*, 36 (2012), 191–198.
11. M. Jabri, E. Mejdoubi, M. El Gadi, B. Hmouti, Optimisation of hardness and setting time of dental zinc phosphate cement using a design of experiments, *Arabian Journal of Chemistry*, 5 (2012), 347-351.
12. A. Rahim, U.K. Sharma, K. Murugesan, A. Sharma, P. Arora, Multi-response optimization of post-fire residual compressive strength of high performance concrete, *Construction and Building Materials*, 38 (2013), 265–273.
13. C.M. Hsu, Cost-based Procedure for Multi-response Parameter design Problems Using GEP, Taguchi Quality Loss, and PSO: Case Study on Heat Sink Design, *International Journal of Computational Intelligence Systems*, 8 (1) (2015), 158-174.
14. M. Khajeh, A. Sarafraz-Yazdi, A.F. Moghadam, Modeling of solid-phase tea waste extraction for the removal of manganese and cobalt from water samples by using PSO-artificial neural network and response surface methodology, *Arabian Journal of Chemistry*, (2013), <http://dx.doi.org/10.1016/j.arabjc.2013.06.011>.
15. Y.T. İç, S. Yıldırım, Improvement of a product design using multi-criteria decision making methods with Taguchi method. *Journal of the Faculty of Engineering and Architecture of Gazi*, 27 (2) (2012), 447-458.
16. T. Yang, P. Chou, Solving a multi-response simulation-optimization problem with discrete variables using a multiple-attribute decision-making method. *Mathematics and Computers in Simulation*, 68 (1) (2005), 9–21.
17. Y. Kuo, T. Yang, G.W., The use of a grey-based Taguchi method for optimizing multi-response simulation problems. *Engineering Optimization*, 40 (6) (2008), 517–528.
18. C.Y. Chang, R. Huang, P.C. Lee, T.L. Weng, R. M. Karp, Determining the optimal mixture for recycled aggregate concrete with multiple responses, *Journal of the Chinese Institute of Engineers*, 37 (2) (2014), 165-174.
19. B. Şimşek, Y. T. İç, E.H. Şimşek, A TOPSIS based Taguchi optimization to determine optimal mixture proportions of the high strength self-compacting concrete. *Chemometrics and Intelligent Laboratory Systems*, 125 (2013), 18-32.
20. T.Y. Chen, Interval-valued fuzzy TOPSIS method with leniency reduction and an experimental analysis. *Applied Soft Computing*, 11 (2011), 4591–4606.
21. C.T. Chen, Extensions of the TOPSIS for group decision-making under fuzzy environment. *Fuzzy Set and Systems*, 114 (1) (2000), 1–9.
22. Y.T. İç, M. Yurdakul, Development of a quick credibility scoring decision support system using fuzzy TOPSIS. *Expert Systems with Applications*, 37 (2010), 567-574.
23. Y.T. İç, Development of a credit limit allocation model for banks using an integrated Fuzzy TOPSIS and linear programming. *Expert Systems with Applications*, 39 (2012), 5309-5316.
24. L.I. Tong, C.T. Su, Optimizing multi-response problems in the Taguchi method by fuzzy multiple attribute

- decision making. *Quality and Reliability Engineering International*, 13 (1997), 25-34.
25. F. Özcan, C.D. Atış, O. Karahan, E. Uncuoğlu, H. Tanyıldızı, Comparison of artificial neural network and fuzzy logic models for prediction of long-term compressive strength of silica fume concrete, *Advance in Engineering Software*, 40 (2009), 856–863.
  26. T.S. Lan, Fuzzy Taguchi deduction optimization on multi-attribute CNC turning. *Transactions of the Canadian Society for Mechanical Engineering*, 34 (2010), 3–4.
  27. S.P. Sivapirakasam, J. Mathew, M. Surianarayanan, Multi-attribute decision making for green electrical discharge machining. *Expert Systems with Applications* 38 (2011) 8370-8374.
  28. A.A. Basma, S. Barakat, S.A. Orami, Prediction of cement degree of hydration using artificial neural networks. *Journal of Materials Chemistry*, 96 (1999), 166–72.
  29. L.D. Graham, D.R. Forbes, S.D. Smith, Modeling the ready mixed concrete delivery system with neural network. *Automation in Construction*, 15 (2006), 656–63.
  30. C. Yeh, Exploring concrete slump model using artificial neural networks, *Journal of Computing in Civil Engineering*, 20 (2006), 217–21.
  31. M. T. Jepsen, *Predicting concrete durability by using artificial neural network* (Published in a special NCR-publication, 2002).
  32. A. Mukherjee, S.N. Biswas, Artificial neural networks in prediction of mechanical behavior of concrete at high temperature. *Nuclear Engineering and Design*, 178 (1997), 1–11.
  33. A. Demir, I.B. Topçu, H. Kusan, Modeling of some properties of the crushed tile concretes exposed to elevated temperatures, *Construction and Building Materials*, 25 (4) (2011), 1883–9.
  34. H. Erdem, Prediction of the moment capacity of reinforced concrete slabs in fire using artificial neural networks, *Advance in Engineering Software*, 41 (2010) 270–9.
  35. N. Al-Metairie, M. Terroand, A. Al-Khaleefi, Effect of recycling hospital ash on the compressive properties of concrete, *Building and Environment*, 39 (2004), 557–66.
  36. J. Bai, S. Wild, J.A. Ware, B. B. Sabir, Using neural networks to predict workability of concrete, *Advance in Engineering Software*, 34 (2003) 663–9.
  37. M. Pala, E. Özbay, A. Öztaş, M.I.Yüce, Appraisal of long-term effects of fly ash and silica fume on compressive strength of concrete by neural networks. *Construction and Building Materials*, 21 (2) (2007), 384–94.
  38. A. Öztaş, M. Pala, E. Özbay, E. Kanca, N. Çağlar, M.A. Bhatti, Predicting the compressive strength and slump of high strength concrete using neural network. *Construction and Building Materials*, 20 (2006), 769–775.
  39. L. Bal, F.B. Bodin, Artificial neural network for predicting drying shrinkage of concrete. *Construction and Building Materials*, 38 (2013), 248–254.
  40. M. Uysal, H. Tanyıldızı, Estimation of compressive strength of self-compacting concrete containing polypropylene fiber and mineral additives exposed to high temperature using artificial neural network. *Construction and Building Materials*, 27 (1) (2012), 404–414.
  41. T. Yang, P. Chou, Solving a multi-response simulation-optimization problem with discrete variables using a multiple-attribute decision-making method. *Mathematics and Computers Simulation*, 68 (1) (2005), 9–21.
  42. EN 206-1, *Concrete- Part 1: Specification, performance, production and conformity*, (Ankara, Turkish Standardization Institute, in Turkish, 2009).
  43. EN 12350/2, *Concrete, Fresh concrete experiments, slump flow test*, (Ankara, Turkish Standardization Institute, in Turkish, 2010).
  44. EN 12390/3, *Testing hardened concrete-Part 3: Compressive strength of test specimens*, (Ankara, Turkish Standardization Institute, in Turkish).
  45. S.J. Chen, C.L. Hwang, *Fuzzy multiple attribute decision making*, (Berlin, Heidelberg, Germany: Springer-Verlag, 1992)
  46. S. M. Phadke, *Quality engineering using robust design*, (New Jersey, Prentice Hall, 1989).
  47. A. R. Yıldız, A new design optimization framework based on immune algorithm and Taguchi's method, *Computers in Industry*, 60 (2009), 613–620.
  48. S. Ballı, S. Korukoğlu, Development of a fuzzy decision support framework for complex multi-attribute decision problems: A case study for the selection of skilful basketball players, *Expert Systems*, 31(1) (2014), 56-69.
  49. H.C. Lin, C.T. Su, C.C. Wang, B.H. Chang, R.C. Juang, Parameter optimization of continuous sputtering process based on Taguchi methods, neural networks, desirability function, and genetic algorithms. *Expert Systems with Applications*, 39 (2010), 12918–12925.
  50. M. Marzouk, M. Elkadi. Estimating water treatment plants costs using factor analysis and artificial neural networks. *Journal of Cleaner Production*, 112 (2016), 4540-4549.
  51. Şimşek B, A Multi-Response Optimization and Modeling Application for Determining Optimal Mix Proportions o Ready-Mixed Concrete: Response Surface Methodology (RSM) with A TOPSIS based Taguchi Approach [dissertation: In Turkish], *Ankara University*, Ankara, 207 p., 2014.